

Sensing-based Resource Allocation In Cognitive Radio Networks

Nafiseh Janatian

Mostly based on

N. Janatian, S. Sun, and M. Modarres Hashemi, "Joint Optimal Spectrum Sensing and Power Allocation in CDMA-based Cognitive Radio Networks," IEEE Trans. Veh. Technol., vol. 64, no. 9, pp. 3990-3998, 2014.

Outline

- Cognitive radio concept
- Two important topics in cognitive radio networks
 - Spectrum sensing
 - Resource allocation
- Sensing based resource allocation in
 - ✓ CDMA-based cognitive radio networks
 - ✗ OFDMA-based cognitive radio networks
- Conclusion and suggestions

Motivation

UNITED STATES FREQUENCY ALLOCATIONS THE RADIO SPECTRUM

RADIO SERVICES COLOR LEGEND

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ACTIVITY CODE

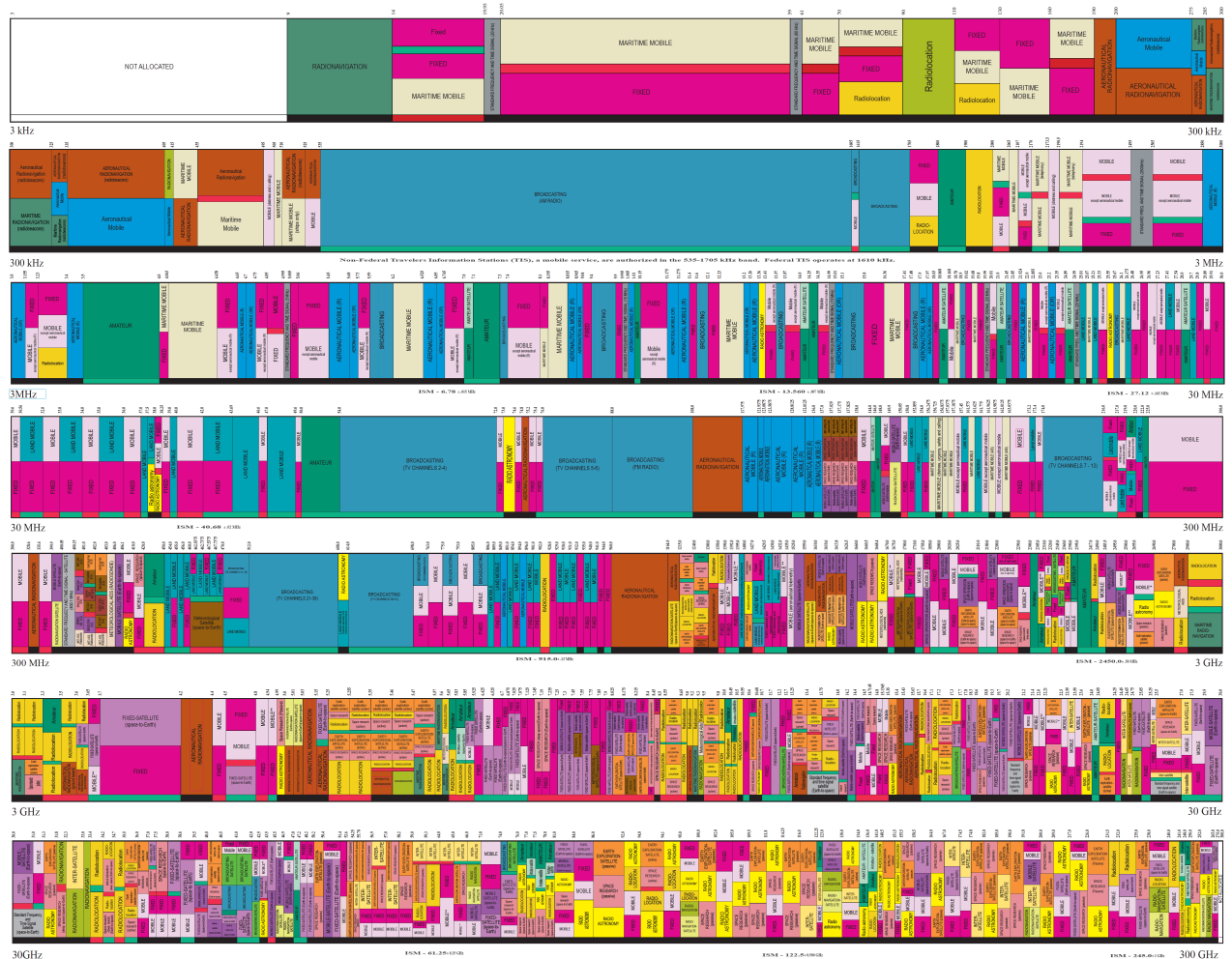
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ALLOCATION USAGE DESIGNATION

SERVICE	EXAMPLE	DESCRIPTION
Primary	FIXED	Capital Letter
Secondary	MAR	1st Capital with Letter over letters

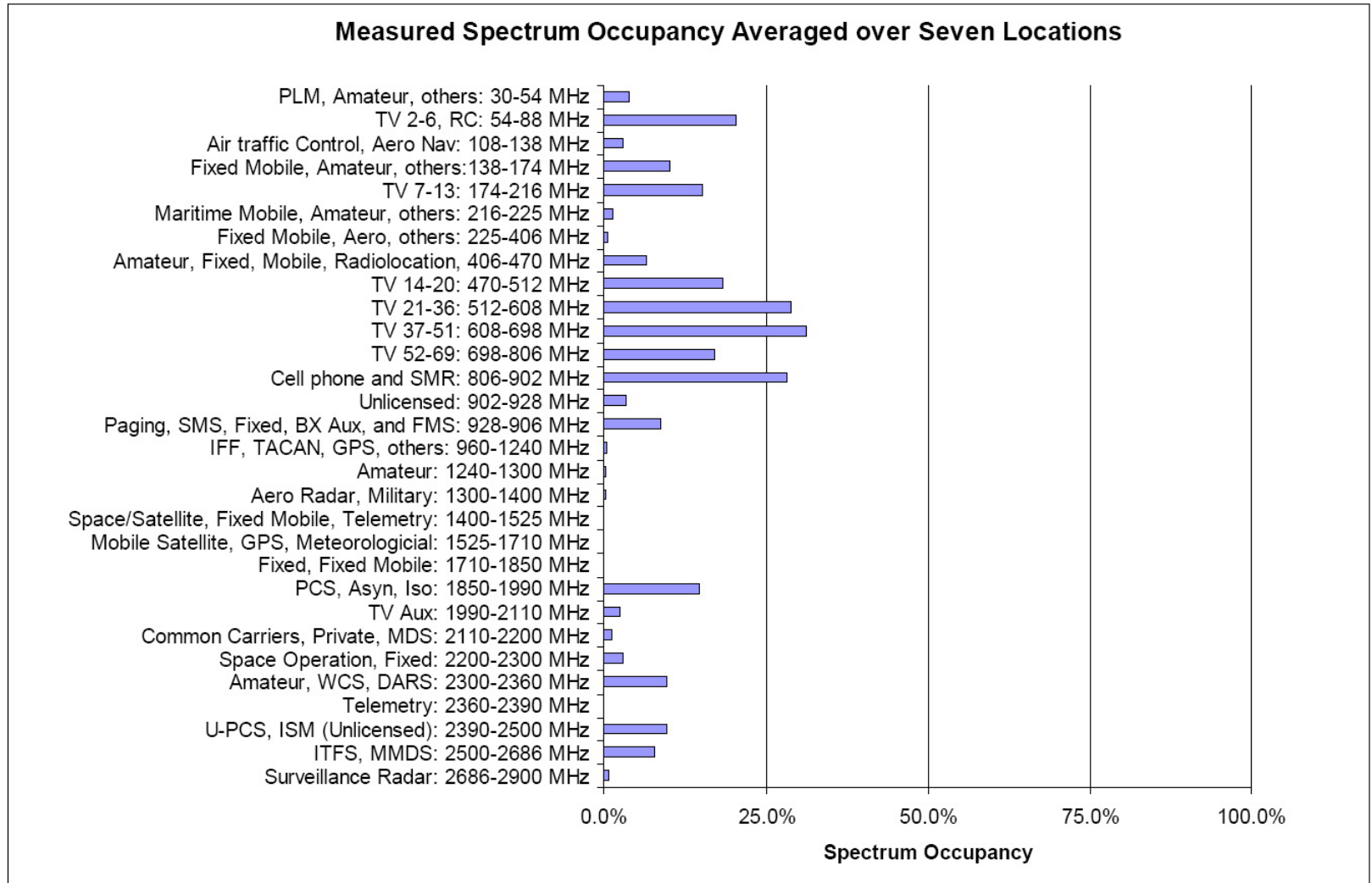
U.S. DEPARTMENT OF COMMERCE
National Telecommunications and Information Administration
Office of Spectrum Management
August 2011

File # 11-081 (Supplemental Chart) 11-11 (Supplemental Chart) 11-12 (Supplemental Chart) 11-13 (Supplemental Chart) 11-14 (Supplemental Chart) 11-15 (Supplemental Chart) 11-16 (Supplemental Chart) 11-17 (Supplemental Chart) 11-18 (Supplemental Chart) 11-19 (Supplemental Chart) 11-20 (Supplemental Chart) 11-21 (Supplemental Chart) 11-22 (Supplemental Chart) 11-23 (Supplemental Chart) 11-24 (Supplemental Chart) 11-25 (Supplemental Chart) 11-26 (Supplemental Chart) 11-27 (Supplemental Chart) 11-28 (Supplemental Chart) 11-29 (Supplemental Chart) 11-30 (Supplemental Chart) 11-31 (Supplemental Chart) 11-32 (Supplemental Chart) 11-33 (Supplemental Chart) 11-34 (Supplemental Chart) 11-35 (Supplemental Chart) 11-36 (Supplemental Chart) 11-37 (Supplemental Chart) 11-38 (Supplemental Chart) 11-39 (Supplemental Chart) 11-40 (Supplemental Chart) 11-41 (Supplemental Chart) 11-42 (Supplemental Chart) 11-43 (Supplemental Chart) 11-44 (Supplemental Chart) 11-45 (Supplemental Chart) 11-46 (Supplemental Chart) 11-47 (Supplemental Chart) 11-48 (Supplemental Chart) 11-49 (Supplemental Chart) 11-50 (Supplemental Chart) 11-51 (Supplemental Chart) 11-52 (Supplemental Chart) 11-53 (Supplemental Chart) 11-54 (Supplemental Chart) 11-55 (Supplemental Chart) 11-56 (Supplemental Chart) 11-57 (Supplemental Chart) 11-58 (Supplemental Chart) 11-59 (Supplemental Chart) 11-60 (Supplemental Chart) 11-61 (Supplemental Chart) 11-62 (Supplemental Chart) 11-63 (Supplemental Chart) 11-64 (Supplemental Chart) 11-65 (Supplemental Chart) 11-66 (Supplemental Chart) 11-67 (Supplemental Chart) 11-68 (Supplemental Chart) 11-69 (Supplemental Chart) 11-70 (Supplemental Chart) 11-71 (Supplemental Chart) 11-72 (Supplemental Chart) 11-73 (Supplemental Chart) 11-74 (Supplemental Chart) 11-75 (Supplemental Chart) 11-76 (Supplemental Chart) 11-77 (Supplemental Chart) 11-78 (Supplemental Chart) 11-79 (Supplemental Chart) 11-80 (Supplemental Chart) 11-81 (Supplemental Chart) 11-82 (Supplemental Chart) 11-83 (Supplemental Chart) 11-84 (Supplemental Chart) 11-85 (Supplemental Chart) 11-86 (Supplemental Chart) 11-87 (Supplemental Chart) 11-88 (Supplemental Chart) 11-89 (Supplemental Chart) 11-90 (Supplemental Chart) 11-91 (Supplemental Chart) 11-92 (Supplemental Chart) 11-93 (Supplemental Chart) 11-94 (Supplemental Chart) 11-95 (Supplemental Chart) 11-96 (Supplemental Chart) 11-97 (Supplemental Chart) 11-98 (Supplemental Chart) 11-99 (Supplemental Chart) 11-100 (Supplemental Chart)

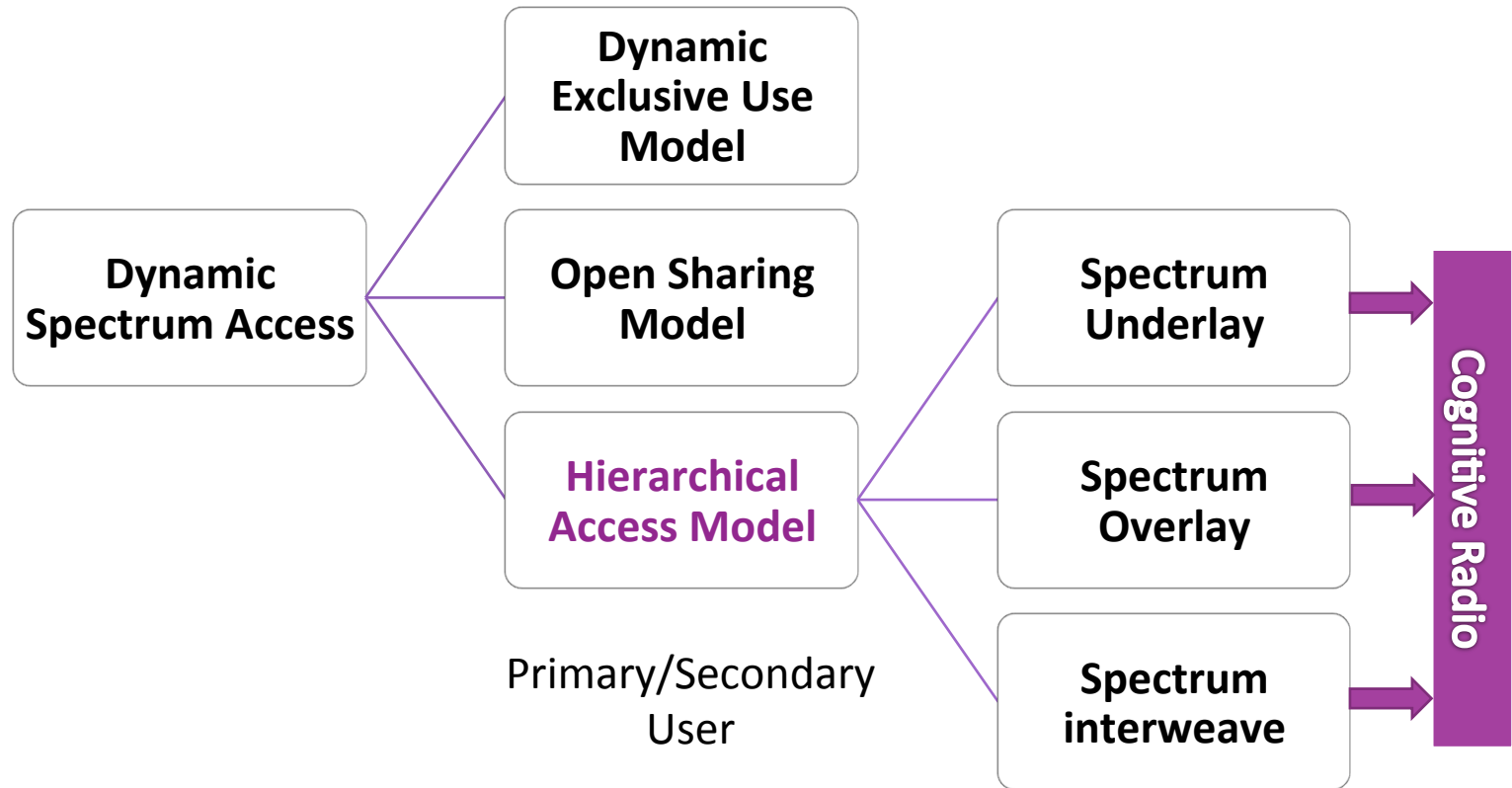


PLEASE REFER TO THE REGULATORY SERVICES IN THE SPECTRUM CHART FOR THE MOST CURRENT INFORMATION. THIS IS AN ALLOCATION OF THE RADIO SPECTRUM.

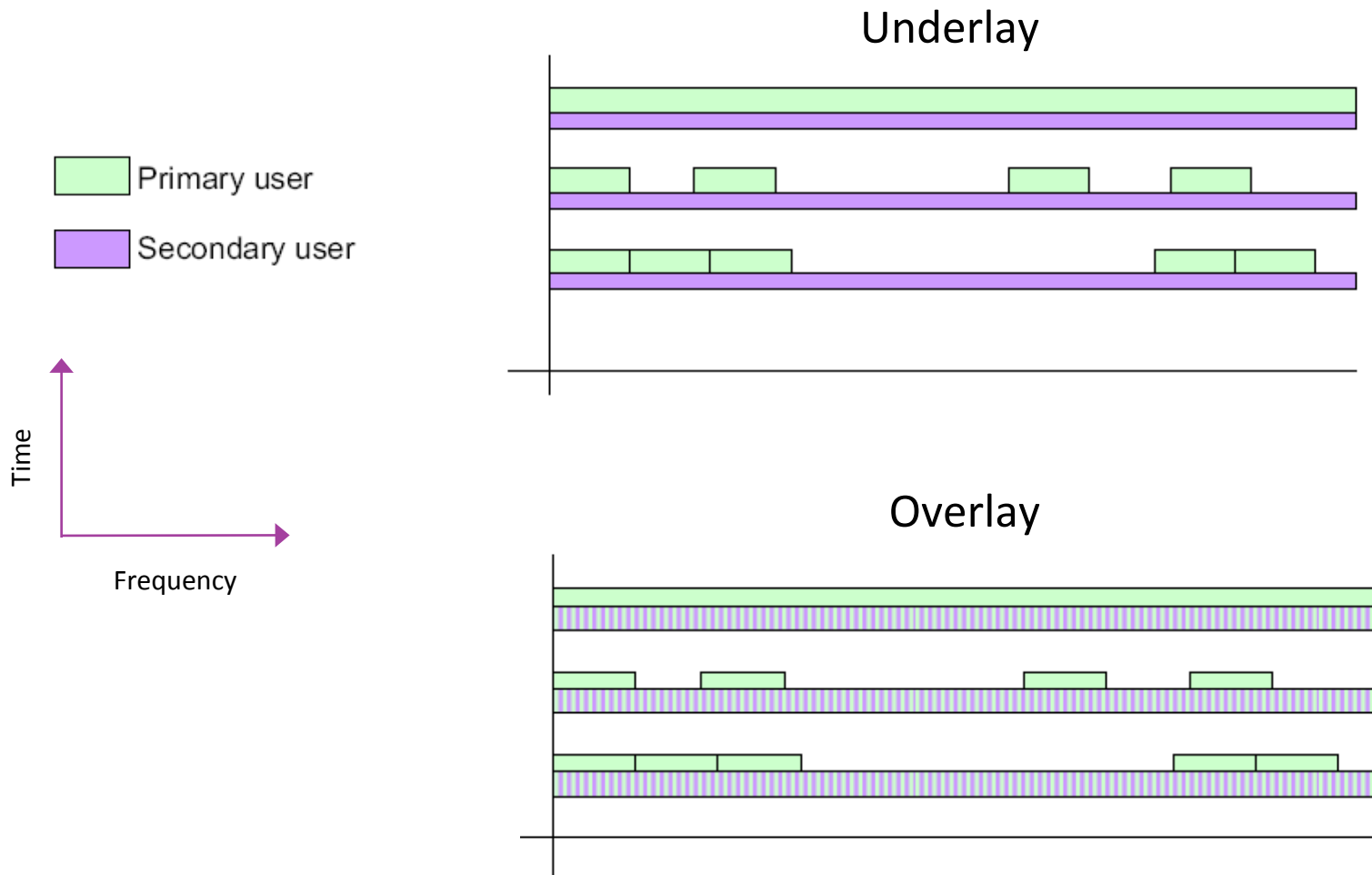
Motivation



Dynamic Spectrum Access

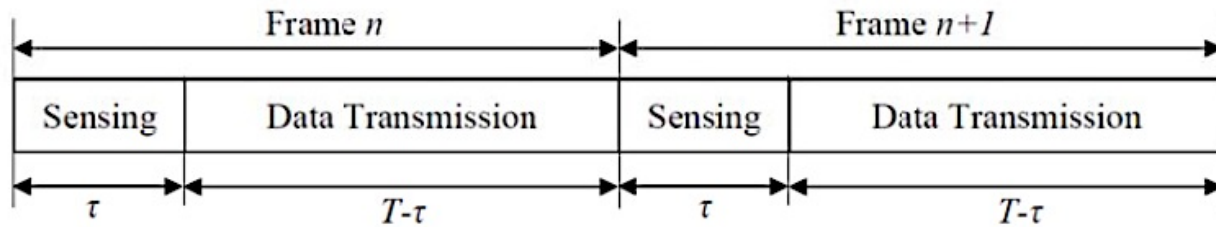
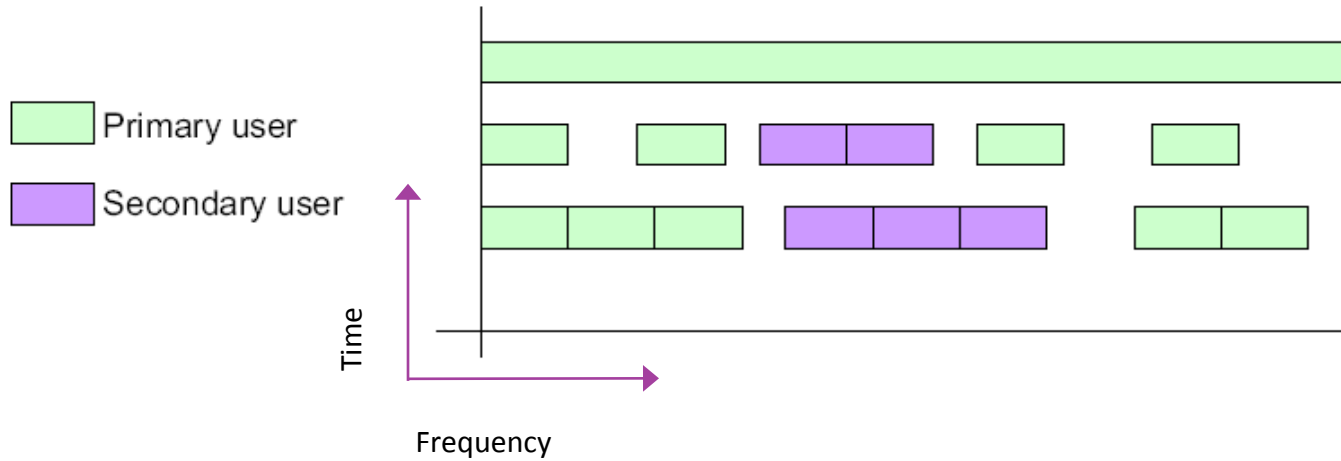


CRN Operation Models



CR Operation Models

Interweave Paradigm



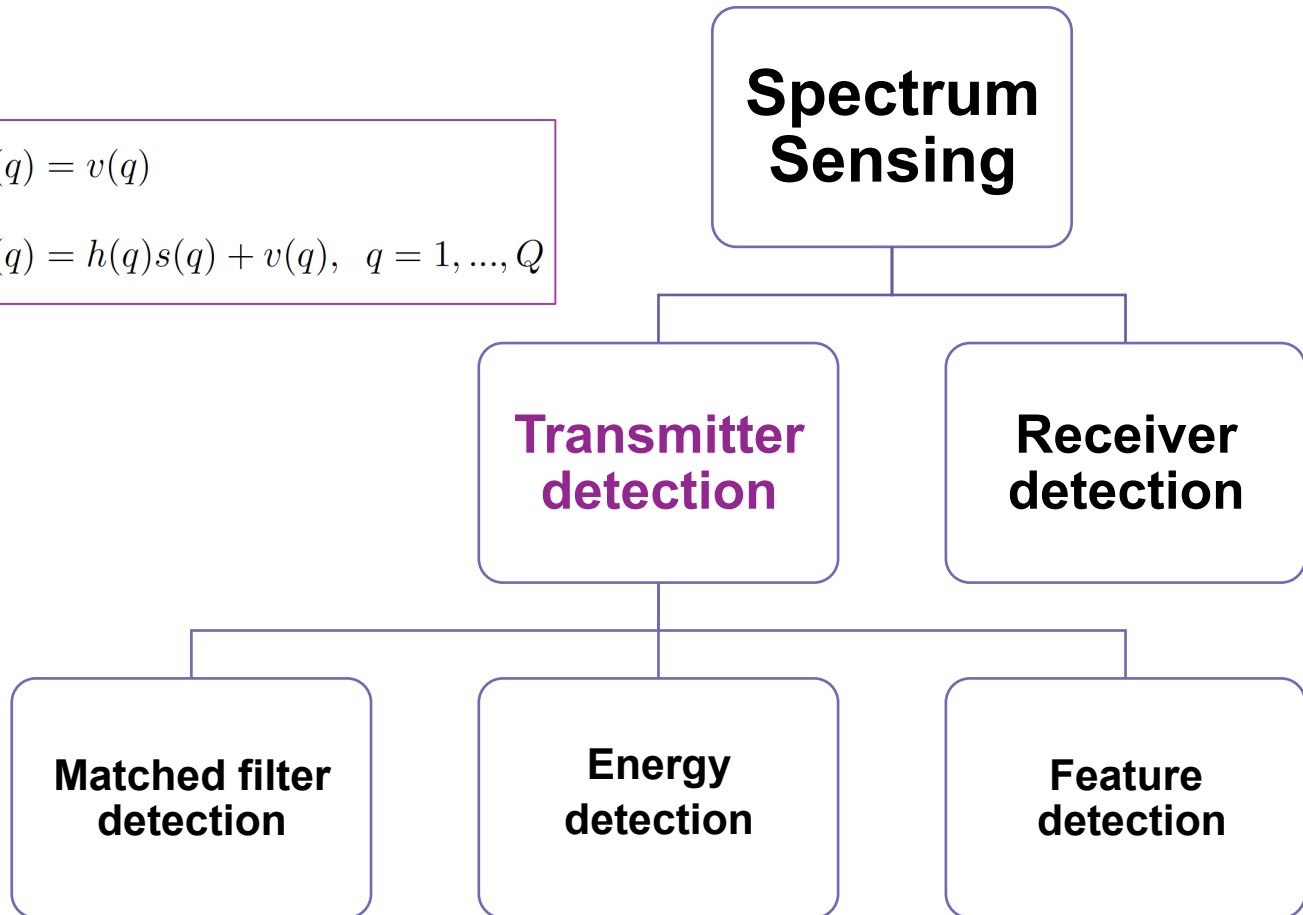
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Spectrum sensing

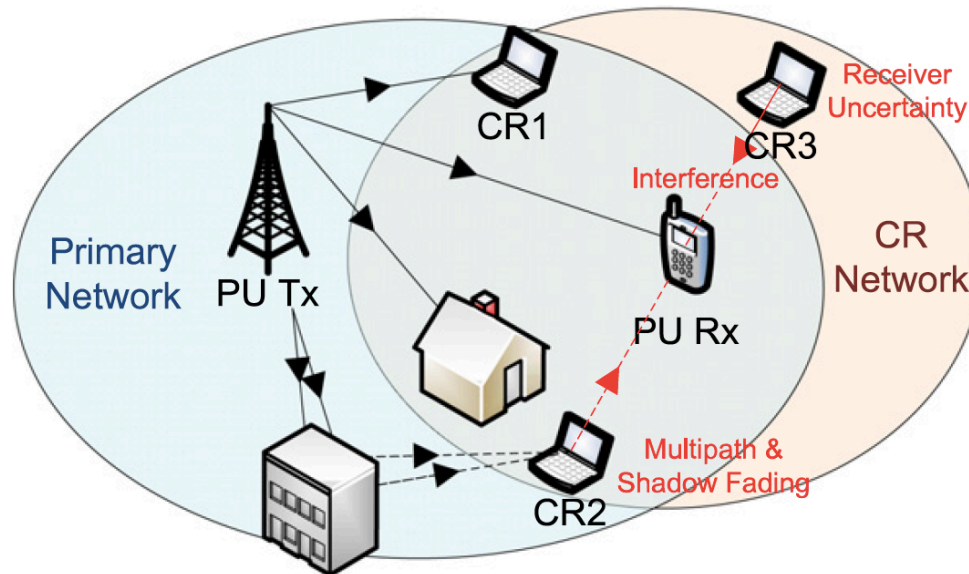
$$H_0 : x(q) = v(q)$$

$$H_1 : x(q) = h(q)s(q) + v(q), \quad q = 1, \dots, Q$$

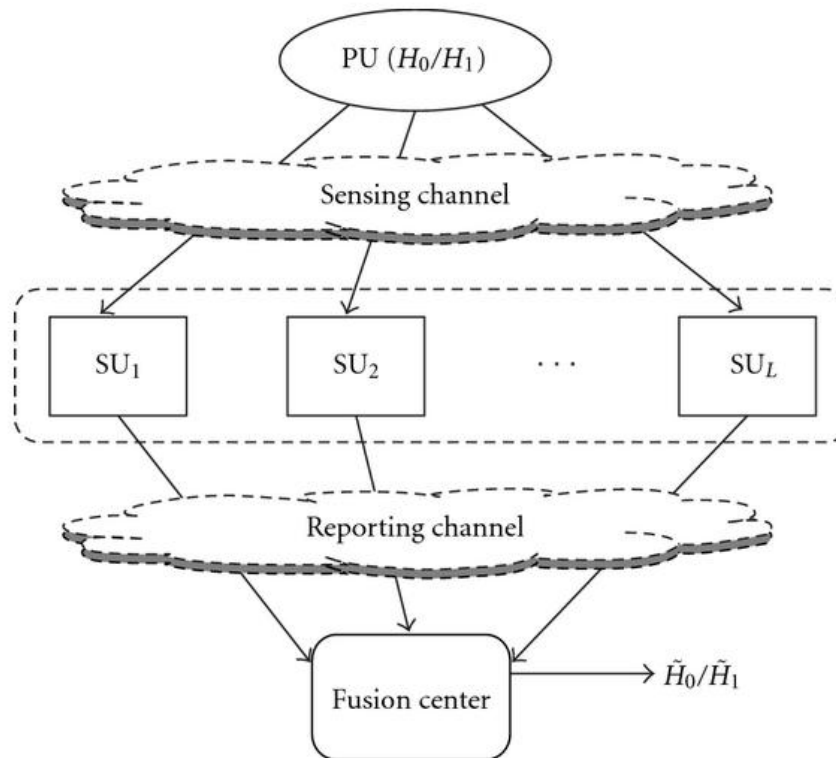


Spectrum sensing

- Performance of Spectrum sensing
 - Pd: Detection probability
 - Pf: False alarm probability
- Spectrum sensing challenges



Cooperative spectrum sensing



- CSS challenges

- Non ideal Sensing and Reporting channels
- Resource efficiency in CSS

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Resource Allocation (RA) in CRNs

- Wireless Resources depending on the technology
 - Frequency bands
 - Time slots
 - Orthogonal codes
 - Transmit power
- RA in **interweave CRNs**
 - **Sensing based Resource Allocation**
 - Maximize the throughput
 - ✓ Minimize the energy consumption
 - Maximize the energy efficiency metric

Energy Consumption Minimization

- Transmit power allocation in a multicarrier-CDMA network with known sensing parameters.

$$\begin{aligned} & \underset{P_i}{\text{Minimize}} && \sum_{i=1}^N \sum_{k=1}^{A_i} P_i^{(k)} \\ & \text{subject to} && (1) \sum_{k=1}^{A_i} P_i^{(k)} \leq P_{max}, \quad i = 1, \dots, N \\ & && (2) \sum_{k=1}^{A_i} b_i^{(k)} \geq R_i, \quad i = 1, \dots, N \\ & && (3) |F_i| = A_i, \quad i = 1, \dots, N \end{aligned}$$

Q. Qi, L. B. Milstein, and D. Vaman, "Cognitive radio based multi-user resource allocation in mobile adhoc networks using multi-carrier CDMA modulation," IEEE J. Sel. Area Comm. , vol. 26, no. 1, pp.70–82, 2008.

Energy Efficiency Maximization

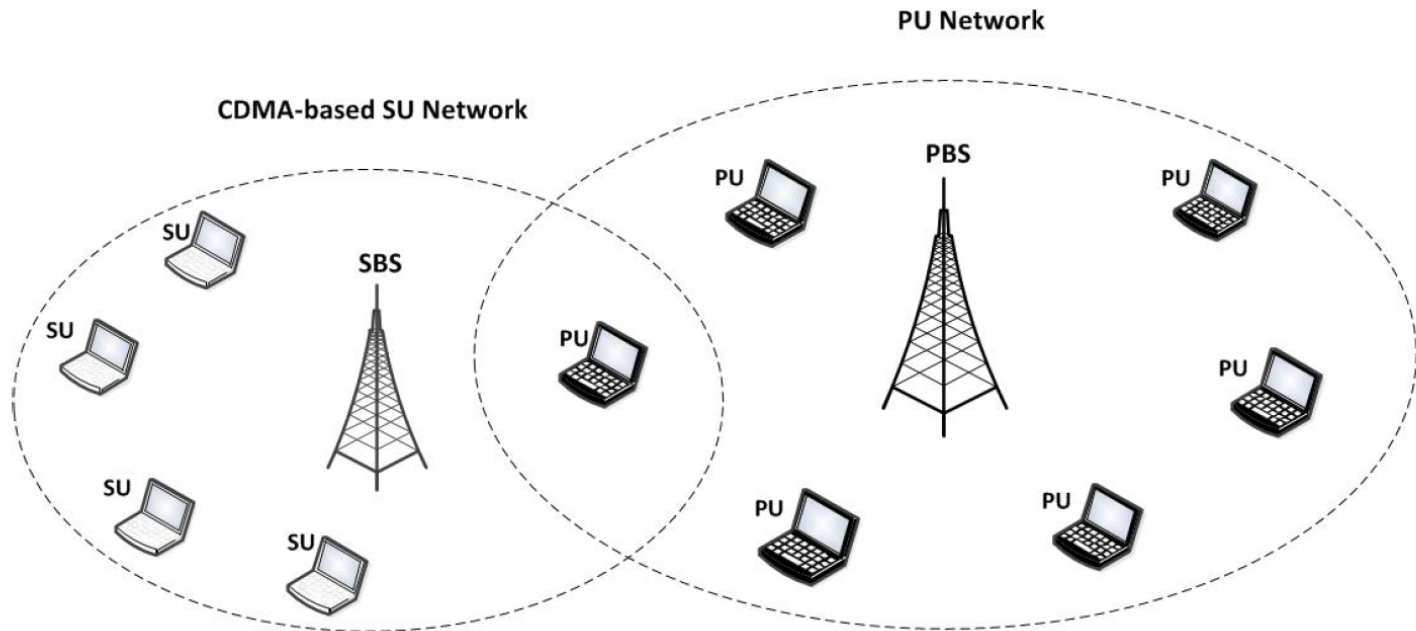
- Sub-channel assignment in CRN consisting M SUs and N sub-channels, with known sensing parameters.

$$\begin{aligned} & \underset{x_{m,n}}{\text{Maximize}} && \eta = \frac{R}{E} \\ & \text{subject to} && (1) \sum_{n=1}^N x_{m,n} \leq 1, \quad m = 1, \dots, M \\ & && (2) \sum_{m=1}^M x_{m,n} \leq 1, \quad n = 1, \dots, N \\ & && (3) x_{m,n} \in \{0, 1\} \end{aligned}$$

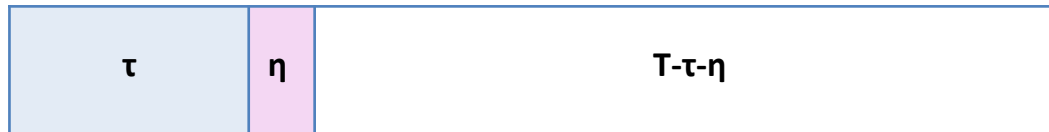
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System Model



Sensing Reporting Channel access



Spectrum sensing phase

- Hypothesis test at the i th SUs

$$x_i(q) \sim \begin{cases} n_i(q) & H_0 \\ n_i(q) + h_i s(q) & H_1 \end{cases}$$

- $s(q)$ is the PU's signal which is assumed to be unknown deterministic
- $n_i(q)$ is the Gaussian noise with zero mean and variance σ_0^2
- $q = 0, \dots, Q - 1$ is the time index, and Q equals τf_s

Spectrum sensing phase

- Energy detector

$$y_i = \frac{1}{\sigma_0^2} \sum_{q=0}^{Q-1} (x_i(q))^2 \sim \begin{cases} \chi_Q^2 & H_0 \\ \chi_Q^2(Q\gamma_i) & H_1 \end{cases}$$

- On-OFF Censoring

$$u_i = \begin{cases} 1 & y_i \geq \lambda_i \\ \times & y_i < \lambda_i \end{cases}$$

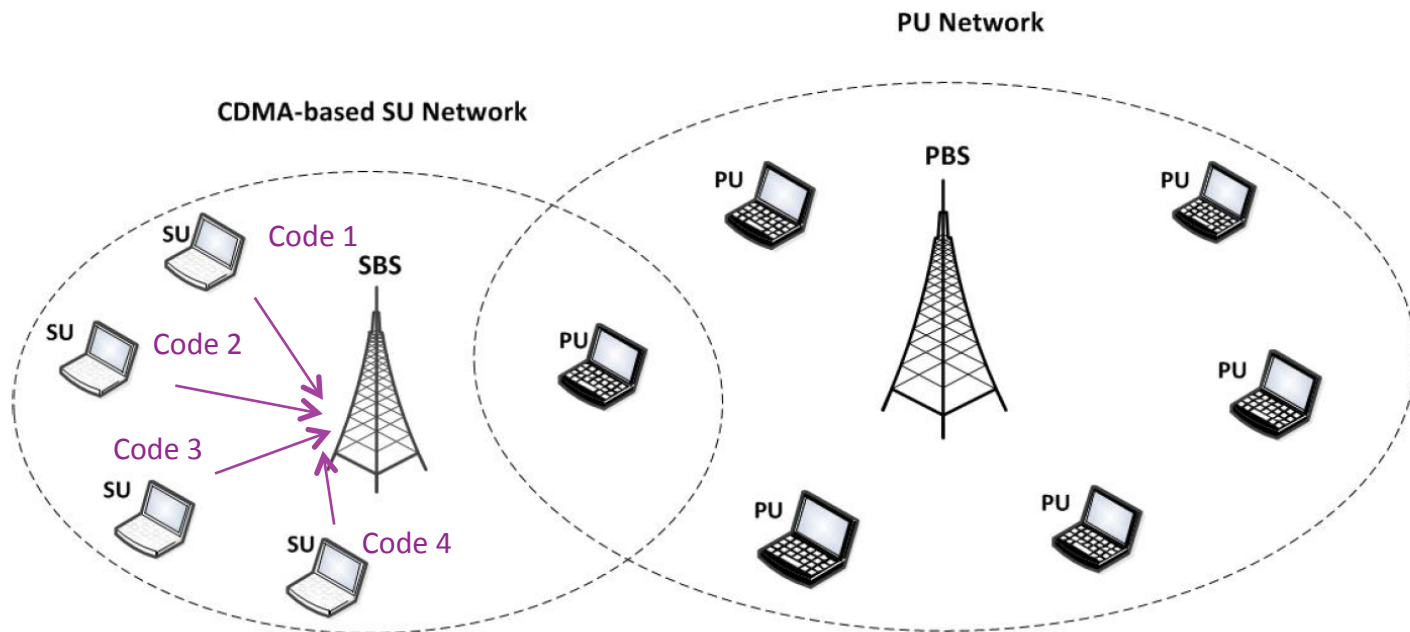
$$P_F = 1 - \prod_{i=1}^M ((1 - p_{f_i})(1 - p_{e_i}) + p_{f_i}p_{e_i})$$

$$P_D = 1 - \prod_{i=1}^M ((1 - p_{d_i})(1 - p_{e_i}) + p_{d_i}p_{e_i})$$

Counting Rule (OR) at Fusion Center

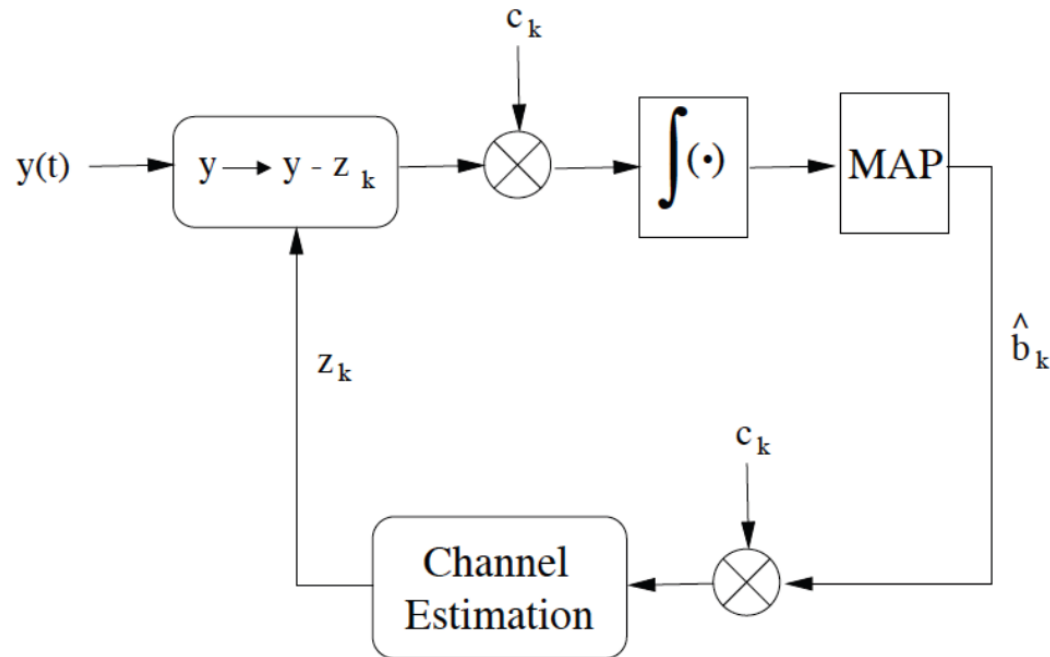
Transmission phase

- Uplink CDMA (Code Division Multiple Access)



Transmission phase

- Conventional single user matched filter
- SIC (Successive Interference Canceller) detector at SBS



Problem Formulation (1)

Joint Optimization of Spectrum Sensing and Power Allocation

Problem P1

$$\begin{aligned} \text{Minimize}_{\Lambda, P} \quad E_T = & \sum_{i=1}^M [(\Phi_{s_i} \tau + \Phi_{r_i} \frac{\eta}{M} ((1 - \rho_{0_i}) \pi_0 + (1 - \rho_{1_i}) \pi_1))] \\ & + (T - \tau - \eta) ((1 - P_F) \pi_0 + (1 - P_D) \pi_1) \sum_{i=1}^M P_i \end{aligned}$$

$$\text{subject to} \quad (1) R_i \approx (1 - \frac{\tau + \eta}{T}) (1 - P_F) \pi_0 \log(1 + \frac{P_i}{\sum_{k=i+1}^M P_k + N_0 W}) \geq \alpha_i$$

$$(2) P_D \geq \bar{P}_D$$

$$(3) P_F \leq \bar{P}_F$$

$$(4) \lambda_i \geq 0, P_i > 0, \quad i = 1, \dots, M$$

Joint optimization

- **Problem P2**

$$\begin{aligned} \text{Minimize}_{p_{f_i}, i=1, \dots, M} \quad E_T = & \sum_{i=1}^M \left[\Phi_{s_i} \tau + \Phi_{r_i} \frac{\eta}{M} (p_{f_i} \pi_0 + p_{d_i} \pi_1) \right] \\ & + N_0 W (T - \tau - \eta) \left((1 - P_F) \pi_0 + (1 - P_D) \pi_1 \right) \\ & \left(\exp \left(\frac{\sum_{i=1}^M \alpha_k}{\pi_0 \left(1 - \frac{\tau + \eta}{T} \right) (1 - P_F)} \right) - 1 \right) \end{aligned}$$

subject to (1) $P_D \geq \bar{P}_D$

(2) $P_F \leq \bar{P}_F$

(3) $0 \leq p_{f_i} \leq 1, \quad i = 1, \dots, M$

- P2 is not convex in general but can be represented as a monotonic optimization problem.

Monotonic Optimization Problem

- Definition :

$$\text{Minimize}\{f(\mathbf{z})|\mathbf{z} \in \mathcal{G} \cap \mathcal{H}\}$$

$$\mathcal{G} = \{\mathbf{z} \in \mathcal{R}_+^n | g(\mathbf{z}) \leq 0\}$$

$$\mathcal{H} = \{\mathbf{z} \in \mathcal{R}_+^n | h(\mathbf{z}) \geq 0\}$$

is a **Monotonic Optimization Problem** iff

- $f(\mathbf{z}), g(\mathbf{z}), h(\mathbf{z}) : \mathcal{R}_+^n \rightarrow \mathcal{R}$ are monotone increasing.
- $\mathcal{G} \cap \mathcal{H} \subseteq [\mathbf{0}, \mathbf{b}] \subseteq \mathcal{R}_+^n$ is a close set.

Joint optimization

- **Problem P3**

$$\text{Minimize}_{p_{f_i}, i=1, \dots, M} \log(E_T) = \log(X_1(\mathbf{p}_f)) + \log(X_2(\mathbf{p}_f))$$

$$\text{subject to} \quad (1) P_D \geq \bar{P}_D$$

$$(2) P_F \leq \bar{P}_F$$

$$(3) 0 \leq p_{f_i} \leq 1, \quad i = 1, \dots, M$$

- $X_2(\mathbf{p}_f)$ is an increasing and $X_1(\mathbf{p}_f)$ is a decreasing function of

$$\mathbf{p}_f = [p_{f_1} \ \dots \ p_{f_M}]$$

- Objective of P3 is a difference of increasing functions and can be represented as a monotonic optimization problem.

Joint optimization

- **Problem P4**

$$\text{Minimize}_{t, p_{f_i}, i=1, \dots, M} t + Y_2(\mathbf{p}_f)$$

$$\text{subject to} \quad (1) t - Y_1(\mathbf{p}_f) \geq -Y_1(\mathbf{1})$$

$$(2) P_D(\mathbf{p}_f) \geq \bar{P}_D$$

$$(3) P_F(\mathbf{p}_f) \leq \bar{P}_F$$

$$(4) 0 \leq p_{f_i} \leq 1, \quad i = 1, \dots, M, \quad 0 \leq t \leq Y_1(0) - Y_1(1)$$

- **Polyblock/Copolyblock** algorithms are suggested by **Tuy** for solving monotonic **Maximization/Minimization** problem.

Problem Formulation (2)

Separate Optimization of Spectrum Sensing and Power Allocation

- **Problem Q1**

$$\underset{p_{f_i}, i=1, \dots, M}{\text{Minimize}} \quad E_{CSS} = \sum_{i=1}^M \left[\Phi_{s_i} \tau + \Phi_{r_i} \frac{\eta}{M} (p_{f_i} \pi_0 + p_{d_i} \pi_1) \right]$$

$$\text{subject to} \quad (1) \quad P_F = 1 - \prod_{i=1}^M ((1 - p_{f_i})(1 - p_{e_i}) + p_{f_i} p_{e_i}) \leq \bar{P}_F$$

$$(2) \quad P_D = 1 - \prod_{i=1}^M ((1 - p_{d_i})(1 - p_{e_i}) + p_{d_i} p_{e_i}) \geq \bar{P}_D$$

$$(3) \quad 0 \leq p_{f_i} \leq 1, \quad i = 1, \dots, M$$

- Monotonic Optimization Problem

Separate Optimization

- **Problem Q2**

$$\text{Minimize}_{\mathbf{P}} \quad E_{Trans} = \left(\sum_{i=1}^M P_i \right) (T - \tau - \eta) \left((1 - P_F)\pi_0 + (1 - P_D)\pi_1 \right)$$

$$\text{subject to} \quad (1) \quad R_i \approx \left(1 - \frac{\tau + \eta}{T} \right) (1 - P_F)\pi_0 \log \left(1 + \frac{P_i}{\sum_{k=i+1}^M P_k + N_0 W} \right) \geq \alpha_i$$

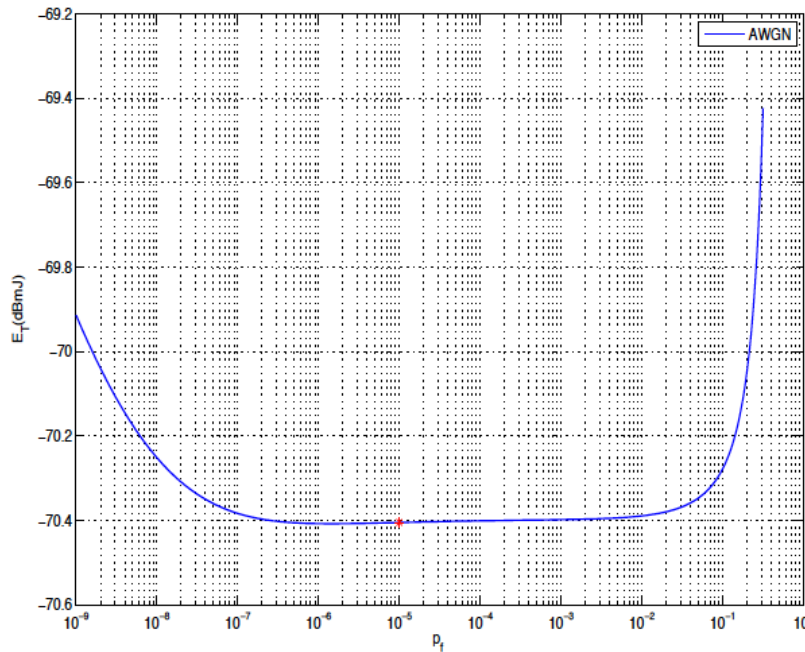
$$(2) \quad P_i > 0, \quad i = 1, \dots, M$$

- Optimal value happens when

$$R_i^* = \alpha_i \quad i = 1, \dots, M$$

Numerical Results

- $M=5, \bar{P}_F = 0.5, \bar{P}_D = 0.95$
- Effect of sensing parameters on energy consumption,



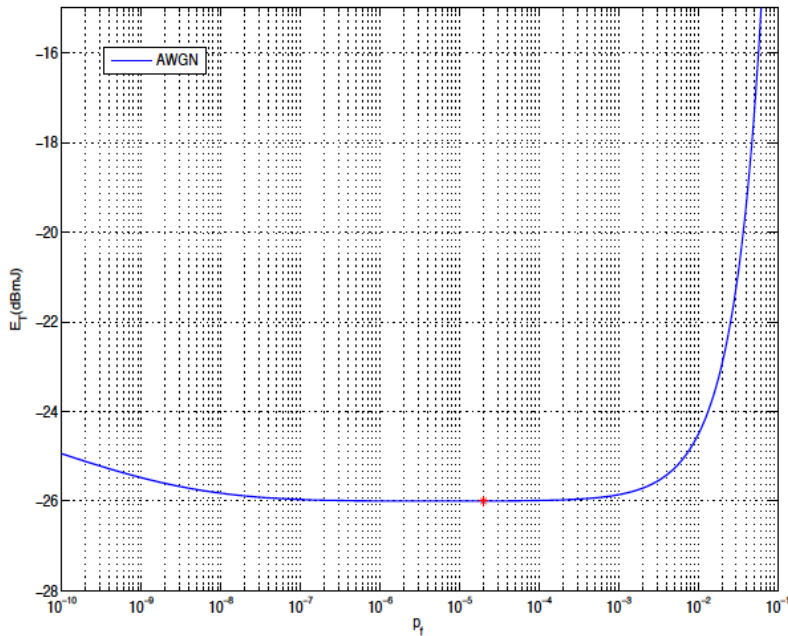
$$\gamma = 0 \text{ dB} \text{ , } \alpha_i = 0.01 \text{ bit/s/Hz}$$

$$\gamma = -5 \text{ dB} \text{ , } \alpha_i = 0.01 \text{ bit/s/Hz}$$

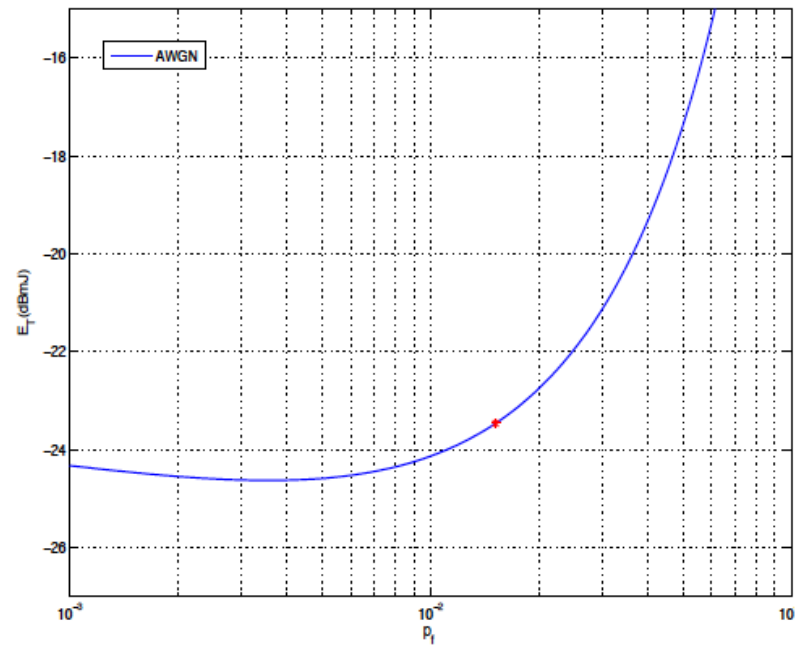


Numerical Results

- Effect of sensing parameters on energy consumption,



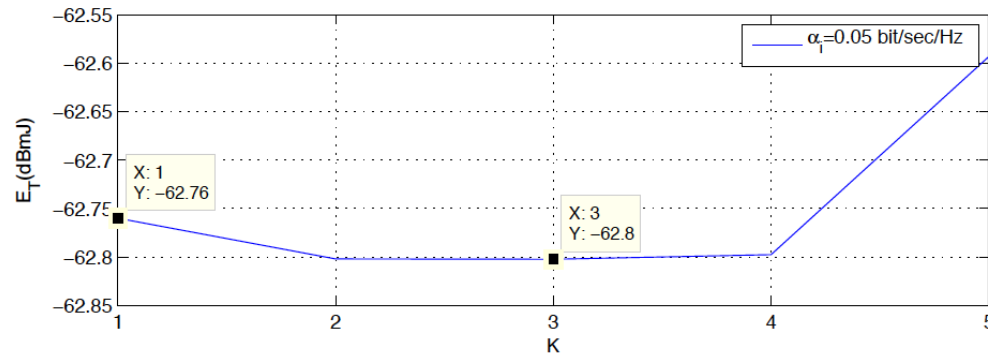
$$\gamma = 0 \text{ dB} \text{ , } \alpha_i = 1 \text{ bit/s/Hz}$$



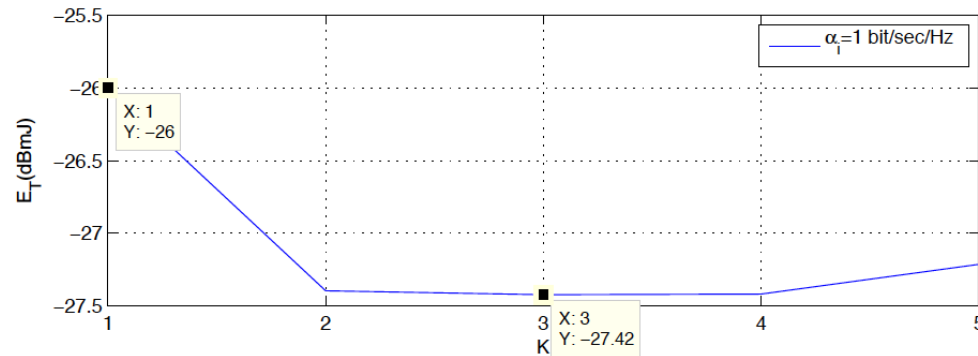
$$\gamma = -5 \text{ dB} \text{ , } \alpha_i = 1 \text{ bit/s/Hz}$$

Numerical Results

- Effect of fusion rule on energy consumption



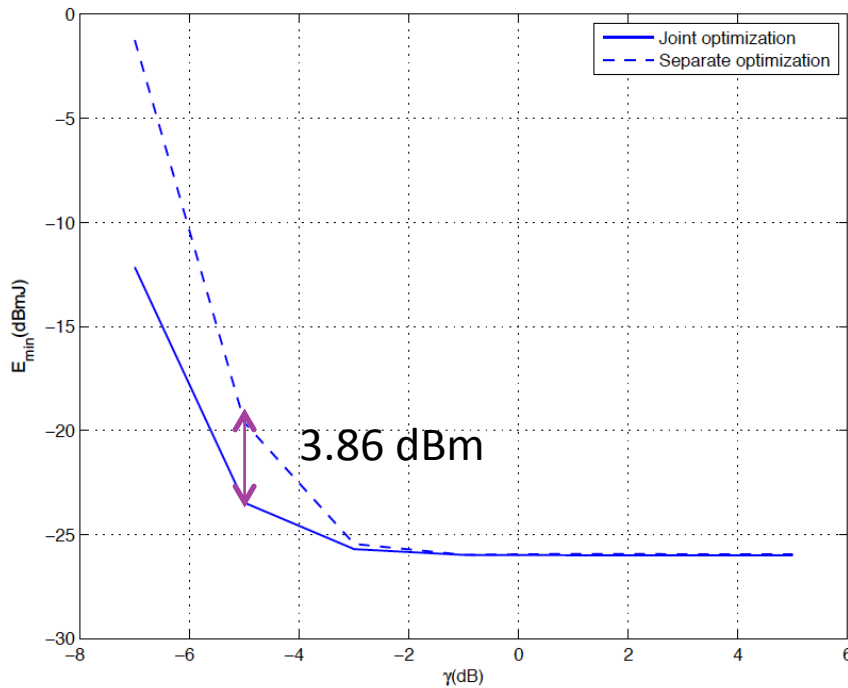
0.04 dBmJ



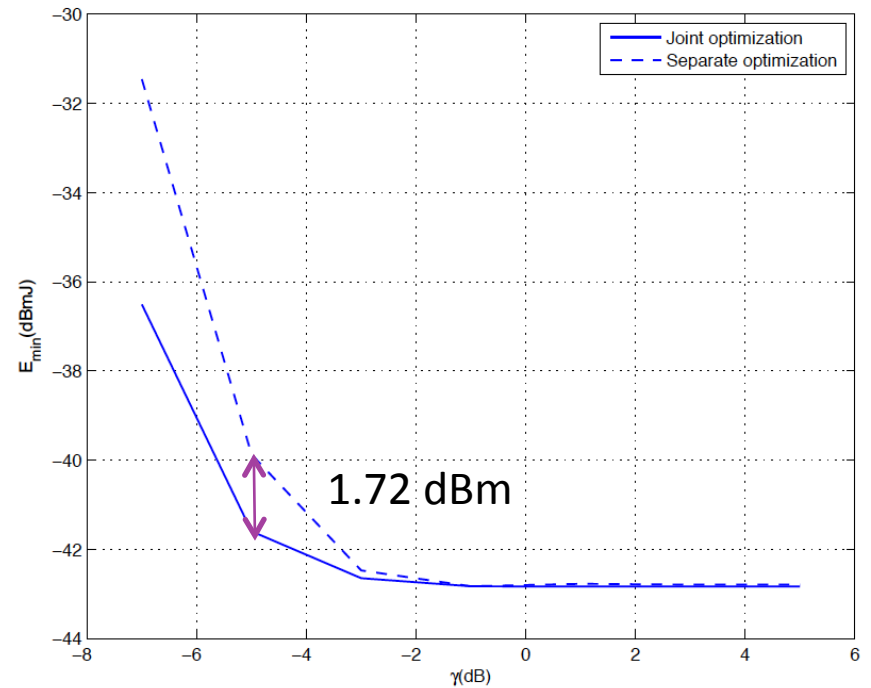
1.42 dBmJ

Numerical Results

- Comparison of joint and separate optimization



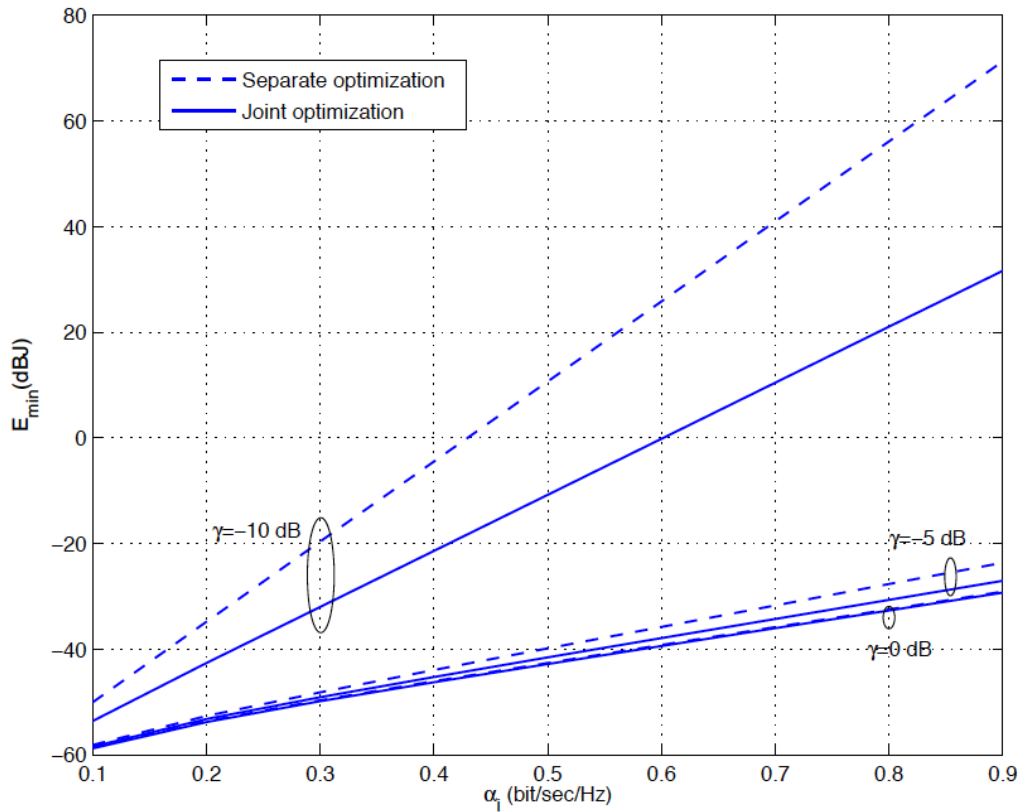
$\alpha_i = 1$ bit/s/Hz



$\alpha_i = 0.5$ bit/s/Hz

Numerical Results

- Comparison of joint and separate optimization



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Conclusion

- Spectrum sensing based resource allocation in CDMA-based cognitive radio networks is considered.
- Joint and separate optimization of sensing parameters and Transmitted powers are studied.
- Numerical results provided suggest that
 - Joint optimization method saves the energy consumption significantly in lower sensing SNRs.
 - It has a very close performance to the separate method in high sensing SNRs

Suggestions

- In this work,
 - uplink power allocation problem for the secondary users,
 - A single channel cognitive radio network with CDMA multiple access of secondary users,
 - Sensing time is fixed.
- Suggestions,
 - The downlink counterpart of the current problem,
 - its extension for the the multi-channel cognitive radio networks,
 - Optimizing the sensing time.

Thanks for your attention!